

Lecture 19

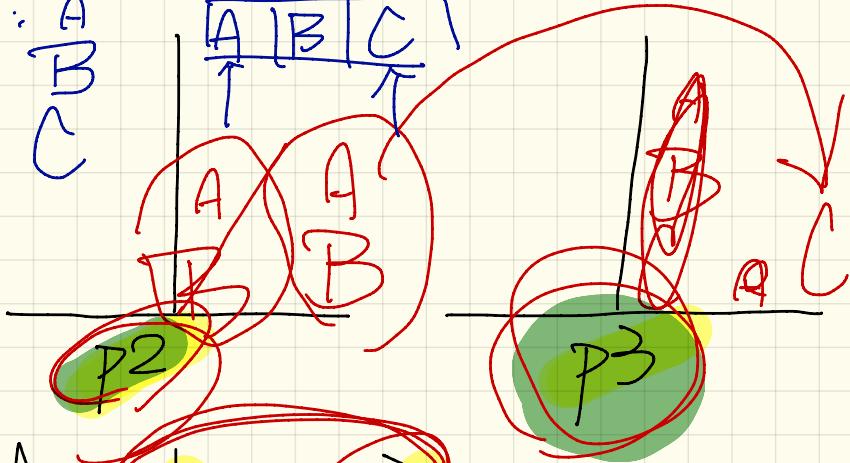
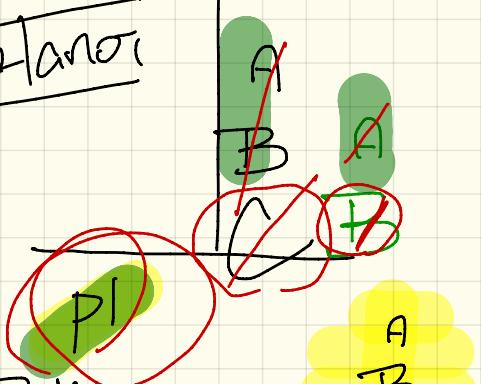
Tuesday Nov. 14

# Tower of Hanoi

Tower:

A  
B  
C

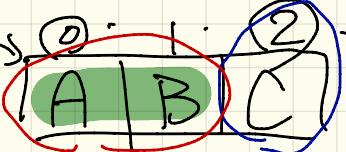
A | B | C  
T T T



Problem: Move C from P1 to P3

- ✓ Move A from P1 to P3
- ✓ Move B from P1 to P2
- ✓ Move A from P3 to P2
- ✓ Move C from P1 to P3
- ✓ Move B from P2 to P3
- ✓ Move A from P2 to P3
- ✓ Move B from P2 to P3

Problem: Move  $\begin{matrix} A \\ B \\ C \end{matrix}$  from  $p_1$  to  $p_3$



$\text{tohH}(ds, 0, 2, p_1, p_3)$   
 { "A", B, C }  
 1 3

$$\text{intermediate} = 6 - 1 - 3$$

$=$

$\text{tohH}(ds, 0, 1, p_1, \underbrace{\text{intermediate}}_{\{A, B\}}, p_3)$

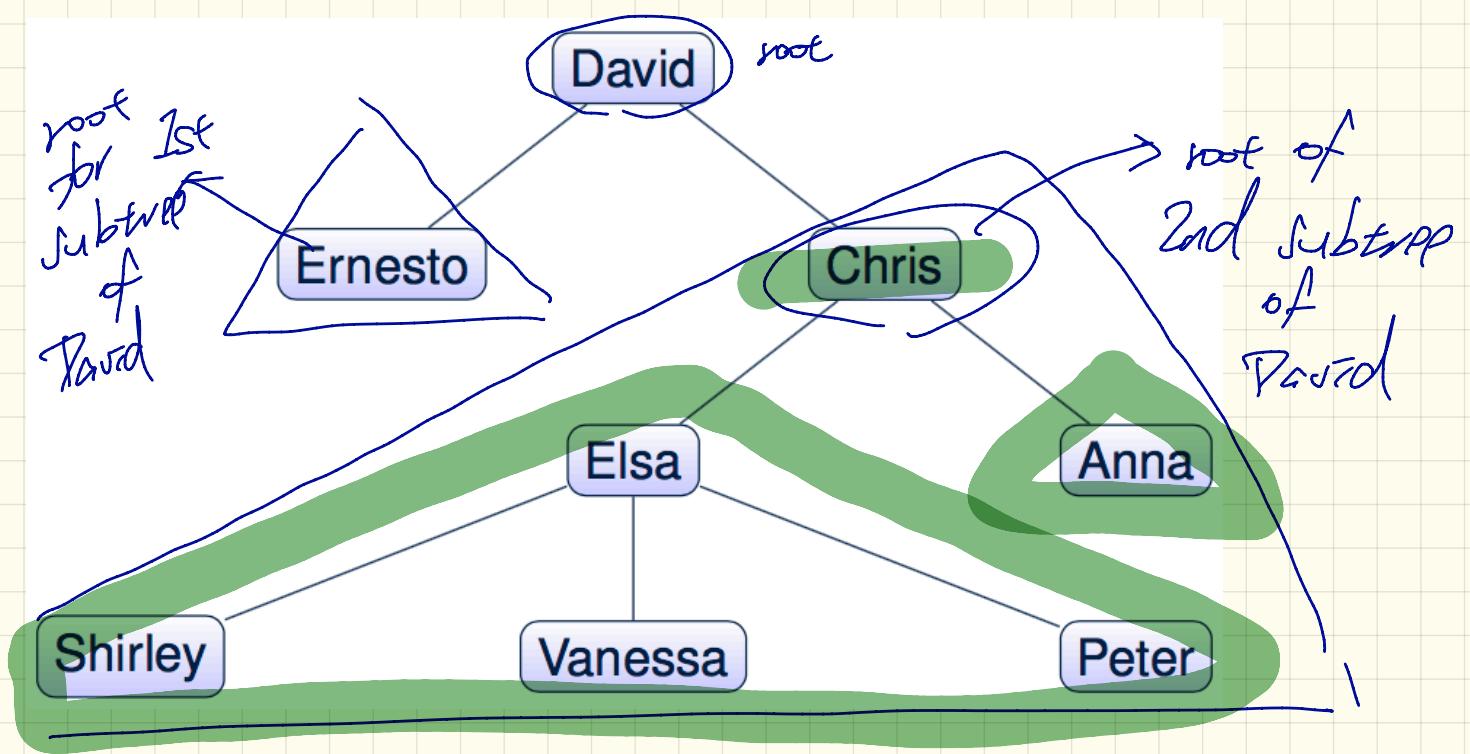
Move  $ds[0]$  from  $p_1$  to  $p_3$

= 2

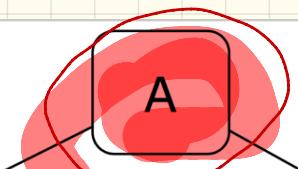
Intermediate:  $p_3$

$\text{tohH}(ds, 0, 1, \text{intermediate}, p_3)$

$\text{tohH}(ds, 0, 0, p_1, p_3)$   
 move  $ds[0]$  from  $p_1$  to  $p_2$   
 $\text{tohH}(ds, 0, 0, p_3, p_2)$



LST of A



root

RST of A

B

C

D

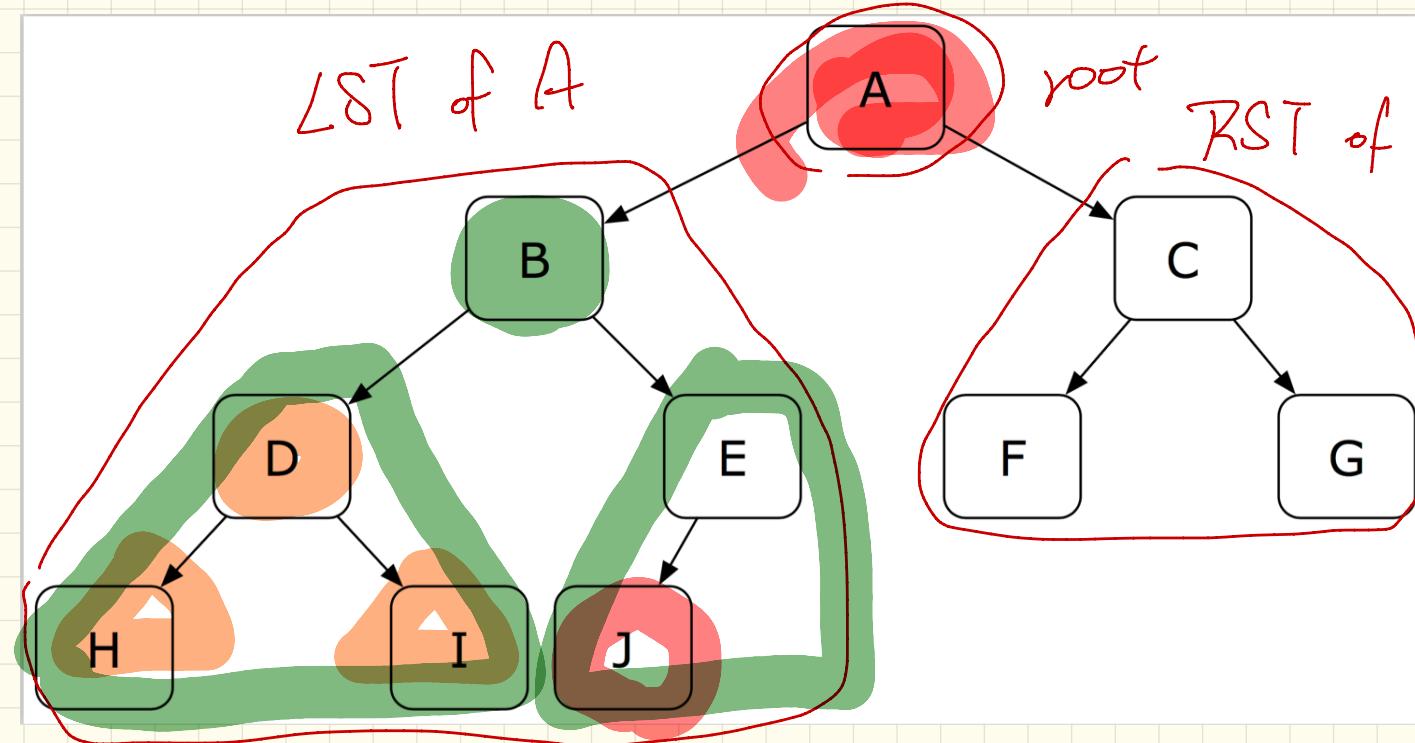
E

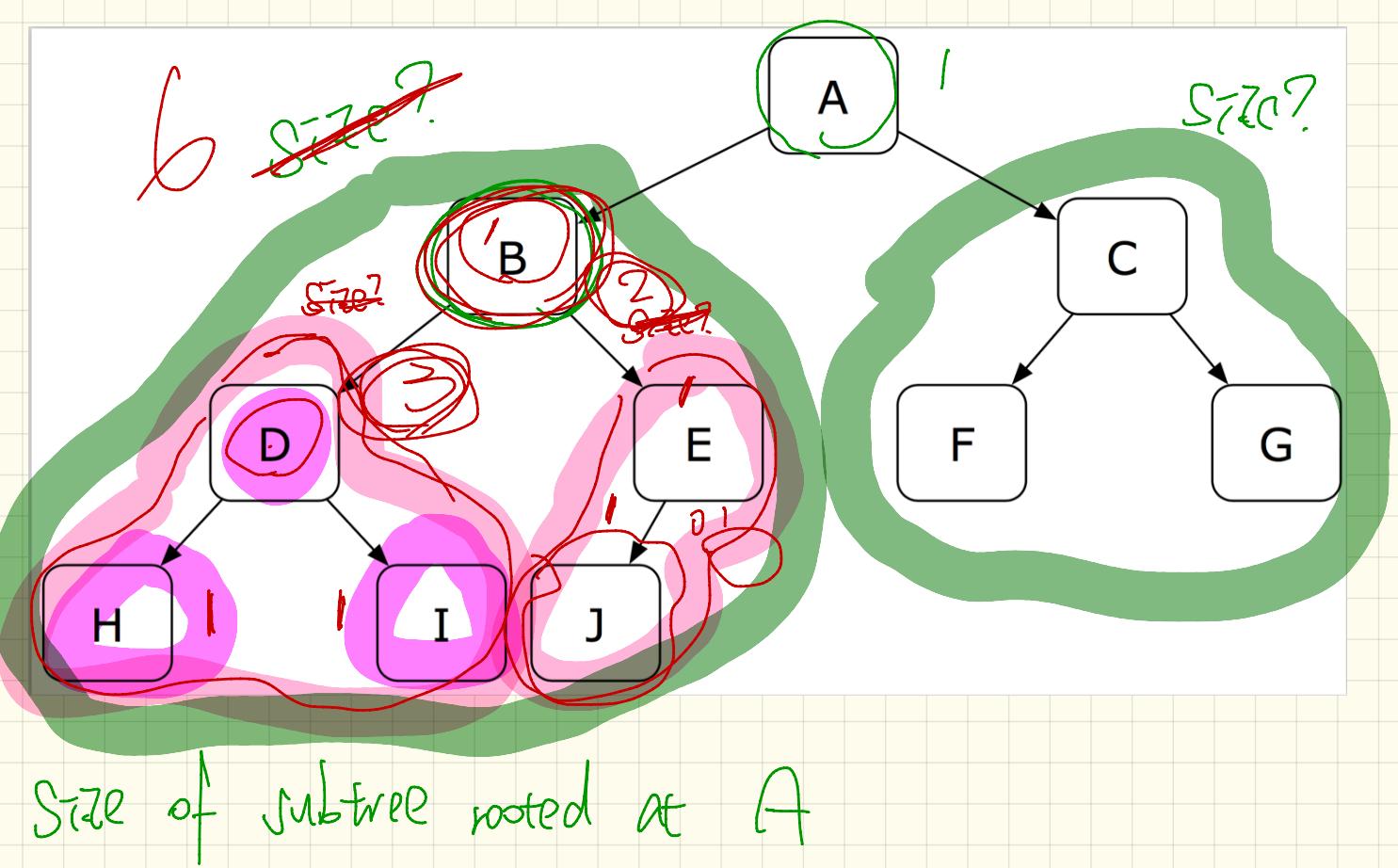
G

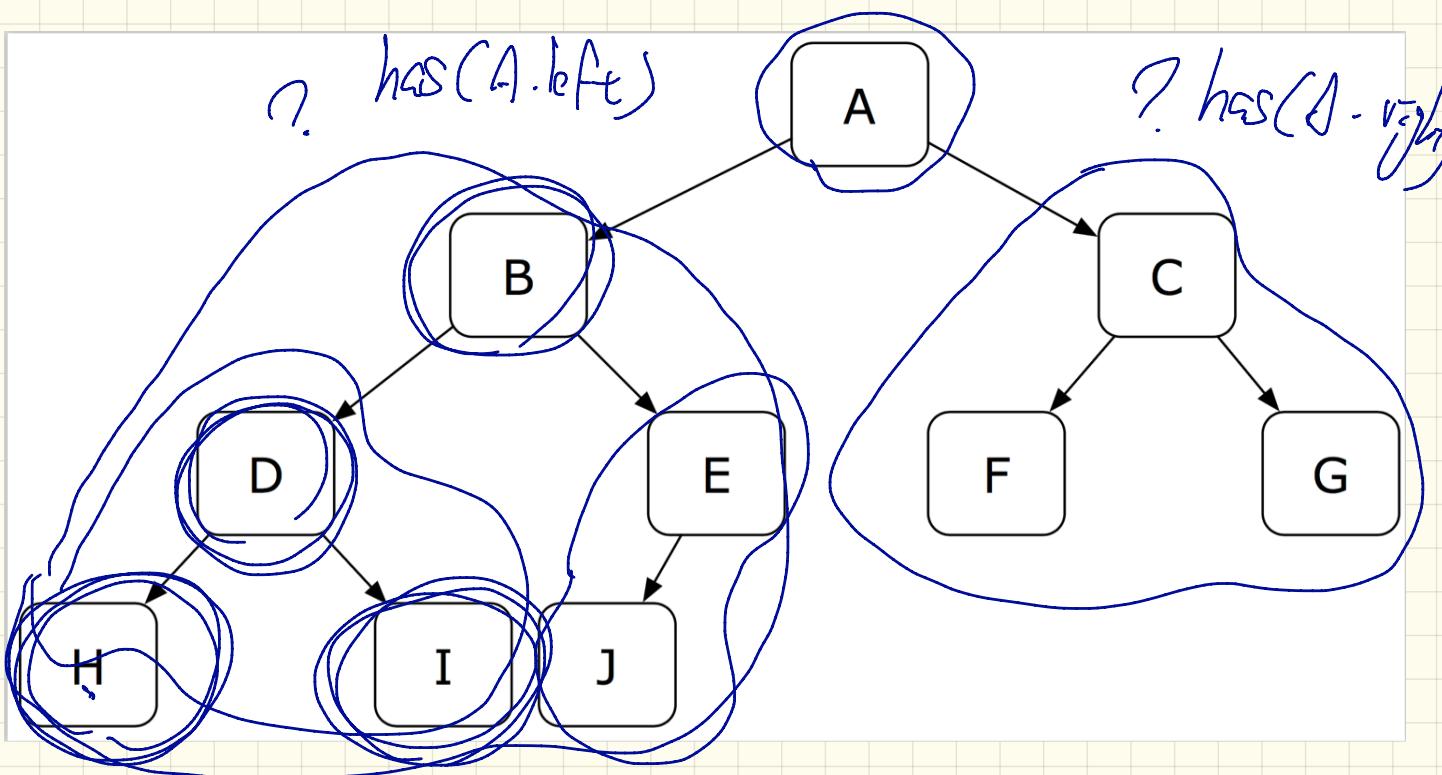
H

I

J







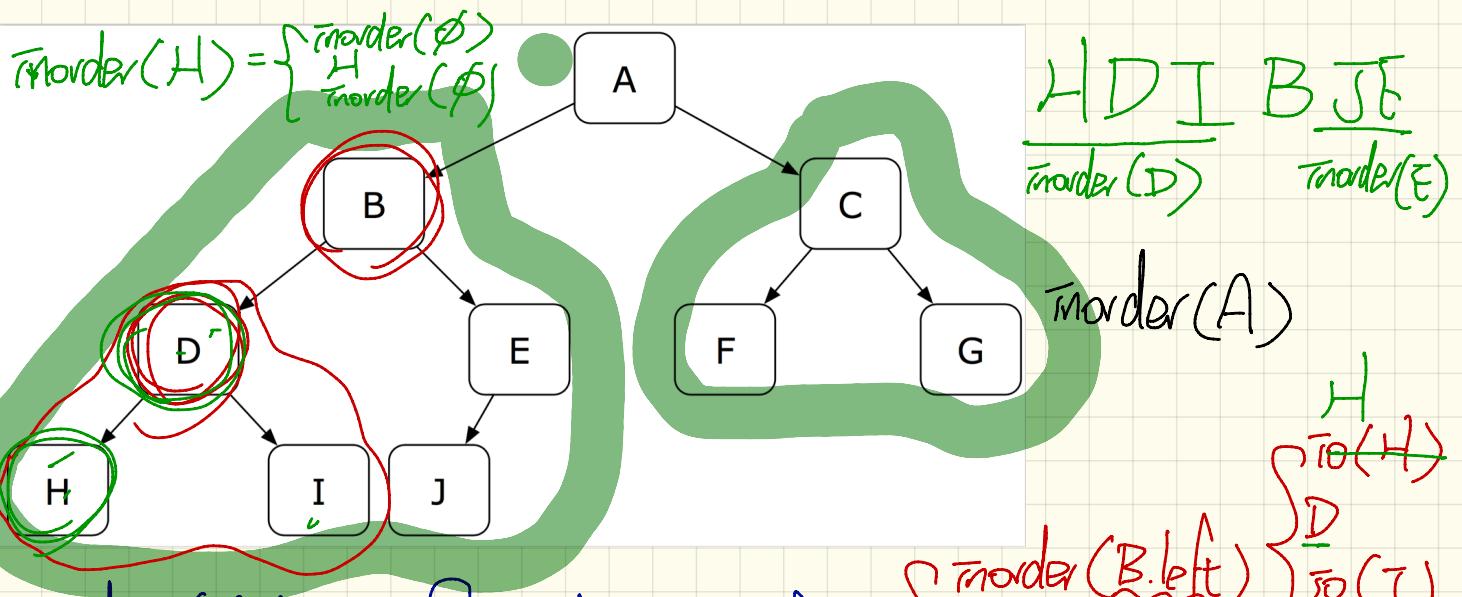
?  $\text{has}(H)$

?  $\text{has}(A)$  =

$$A == H \quad ||$$

$$\text{has}(A.\text{left}) \quad ||$$

$$\text{has}(A.\text{right}).$$



$$\frac{HDI}{\text{inorder}(D)} \quad \frac{BJE}{\text{inorder}(E)}$$

$$\text{inorder}(A)$$

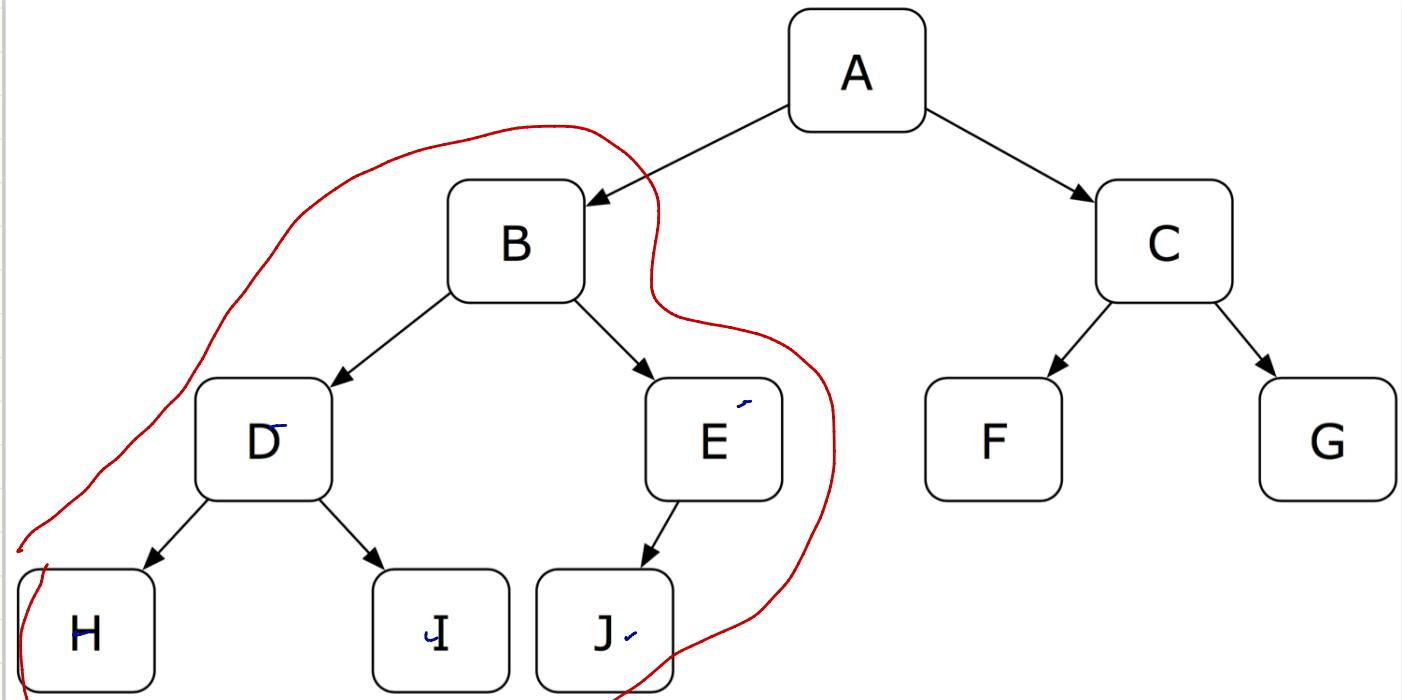
$$H \\ \text{inorder}(H)$$

$$D \\ \text{inorder}(D)$$

$$I \\ \text{inorder}(I)$$

$\text{inorder}(A) = \{ \text{inorder}(A.\text{left}), B, \text{inorder}(A.\text{right}) \}$

$B = \{ \text{inorder}(B.\text{left}), B, \text{inorder}(B.\text{right}) \}$



$\text{inorder}(A)$

$\overline{\text{in}}(B)$

$\overline{\text{in}}(A)$

$\boxed{H D I \cancel{B} J E}$   $\cancel{A} \overline{\text{in}}(F C G)$   
 $\overline{\text{in}}(D)$   $\overline{\text{in}}(E)$   $\overline{\text{in}}(C)$